

## Chapter 7

### Biaxial Optics

## Biaxial mineral

- Include orthorhombic, monoclinic and triclinic crystal systems.
- 대칭률이 uniaxial mineral보다 낮음
- 모든 방향에 대해 다양한 결정 구조와 화학 결합을 갖는다
- 세 축의 길이가 모두 다름 = 3개의 서로 다른 굴절률을 갖음( $\alpha, \beta, \gamma$ ) : 축간의 사이각과 혼란을 피하기 위해  $n$ 을 붙여 씀

## Biaxial minerals

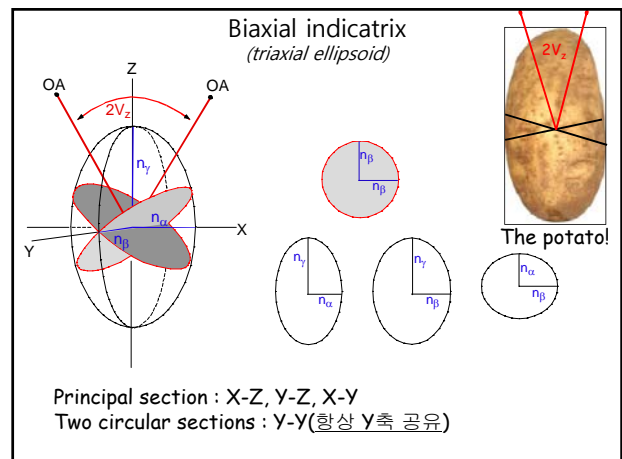
- $n_a, n_b, n_c = n_\alpha, n_\beta, n_\gamma = N_x, N_y, N_z = nX, nY, nZ = X, Y, Z = n_1, n_2, n_3 = n_p, n_m, n_g$
- $n_\alpha < n_\beta < n_\gamma$
- The maximum birefringence of a mineral is always =  $n_\gamma - n_\alpha$

## Biaxial minerals

- 혼돈을 피하기 위한 방법
  - 이방성 광물을 통과하는 빛은 하나는 fast ray, 다른 하나는 slow ray로 갈라짐
  - Ordinary/extraordinary terminology(용어)가 이방성 광물에서는 쓰이지 않는다. 여기서 2개의 ray는 모두 일축성 광물에서 extraordinary ray와 동일
- Slow ray 굴절률 :  $n_\gamma'$  ( $n_\beta \leq n_\gamma' \leq n_\gamma$ )
- Fast ray 굴절률 :  $n_\alpha'$  ( $n_\alpha \leq n_\alpha' \leq n_\beta$ )

## Biaxial indicatrix

- Uniaxial mineral과 동일한 방법으로 작도되고 유사한 방법으로 해석됨
- 주된 차이점 : indicatrix의 세 축의 길이가 모두 다르다.
- 세 축의 길이 = principal indices of refraction, 통과하는 빛의 굴절률, 진동방향
- 광물의 축은 직각이 아니더라도 indicatrix의 축은 항상 수직이 되도록 작도함



1. In the X-Z plane :  $n_\alpha \leq n_{\alpha'} \leq n_\beta \leq n_{\gamma'} \leq n_\gamma$   
 2. X-Z plane 에서  $n_\beta$  와 동일한 반경을 지시하는 직선의 수직선 = Optic axis(OA)  
 3. OA는 X-Z plane에서 두 개가 발생함  
 4. 두 OA 사이의 각도 = **2V angle** or **Optic angle**  
 5. X-Z plane은 OA를 포함하고 있기 때문에 Optic plane이라고도 불림

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Looking down true  $\beta$

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### Biaxial Crystals

**Nomenclature:**

- 2 circular sections → 2 optic axes
- Must be in  $\alpha$ - $\gamma$  plane = **Optic Axial Plane (OP)**
- $Y \parallel \beta$  direction  $\perp$  OP = **optic normal**

Acute angle between OA's = 2V  
 The axis that bisects acute angle = **acute bisectrix = Bxa**  
 The axis that bisects obtuse angle = **obtuse bisectrix = Bxo**

### Biaxial Positive and Negative

Looking down true  $\beta$

**B(+)** defined as Z ( $\gamma$ ) = Bxa  
 Thus  $\beta$  closer to  $\alpha$  than to  $\gamma$   
 $2V_x > 90^\circ$ ,  $2V_z < 90^\circ$

Looking down true  $\beta$

**B(-)** defined as X ( $\alpha$ ) = Bxa  
 Thus  $\beta$  closer to  $\gamma$  than to  $\alpha$   
 $2V_x < 90^\circ$ ,  $2V_z > 90^\circ$

Alas, the potato (indicatrix) can have any orientation within a biaxial mineral...

olivine

augite

- In the special case where  $2V$  is exactly  $90^\circ$ , the mineral is optically neutral.
- 이러한 명명법은 특히 화학적 성분의 변화로써 광학적으로 positive에서 negative까지 변화하는 광물을 위한 광학적 data를 표현하는데 유용하다.
- Uniaxial indicatrix는 biaxial indicatrix의 특수한 경우로 생각되는 수도 있다
  - $n_a = n_b$  일 경우 : Z 축 = OA, X-Y plane = circular section(uniaxial positive)
  - $n_b = n_c$  일 경우 : X 축 = OA, Y-Z plane = circular section(uniaxial negative)

### Use of the indicatrix

- Uniaxial indicatrix와 동일
- 작도시 좀더 주의 요망(WN : wave normal)
- Ray 작도 : page 79 참조

Figure 7.4 Determining indices of refraction and vibration directions given the wave normal direction. (a) Uniaxial indicatrix with wave normal (WN) and elliptical section perpendicular to the wave normal. The axes of the elliptical section ( $n_x$  and  $n_y$ ) indicate the vibration directions and indices of refraction of the slow and fast rays. (b) Ray directions associated with the wave normal. Tangents to the indicatrix are constructed through the wave normal and parallel to the axes of the elliptical section. The points of tangency  $a$  and  $b$  indicate where the slow and fast rays emerge from the indicatrix.

### Biot-Fresnel Rule

WN과 관련된 진동 방향을 결정하기 위해 이용  
WN과 OA를 포함하는 두면을 작도  
WN을 통과하는 빛의 진동방향 : 두 면사이의 각도를 2등분 함

Figure 7.5 Biot-Fresnel construction. The vibration directions (arrows) associated with the wave normal (WN) bisect the angles between planes constructed from the optic axis (OA) to the wave normal.

- ### 광물을 통과하는 빛의 유형
- Case 1 : 3축중 하나에 평행하게 빛이 입사
  - Case 2 : OA에 평행하게 입사
  - Case 3 : 불규칙하게 입사
  - Case 4 : 경사져서 입사(WN 자체가 굴절됨 - 생략)

### Case 1 : 3축중 하나에 평행하게 빛이 입사

Figure 7.6 Normal incidence parallel to the Z indicatrix axis. The two rays vibrate parallel to the X and Z indicatrix axes and have indices  $n_x$  and  $n_z$ .

- 통과 빛의 굴절률 : 타원의 장축
- WN // ray path

### Case 2 : OA에 평행하게 입사

Figure 7.7 Normal incidence parallel to an optic axis. (a) Section through the indicatrix in a circular section, so all light has index  $n_o$  with no preferred vibration directions. The wave normal for all light follows the optic axis. Ray paths such as  $1, 2, 3$  form a hollow cone of light within the mineral and a hollow cylinder along the normal. (b) Vibration directions for light in the cone. (See text for more information.)

- Indicatrix 단면 : 원
- WN과 ray 경로가 평행하지 않음
- Cone 형태의 빛 발산(비편광 입사시)

- 작도는 Fig. 7.4와 동일한 방식으로 작도
- 위 그림은 약간 과장되게 표현한 것임 - 실제로는 Cone radius가 매우 작음(항상 검게 보임)

### Case 3 : 불규칙하게 입사

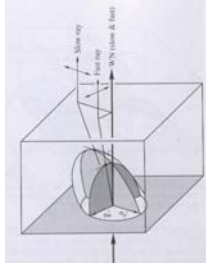


Figure 7.8 Normal incidence to a crystal plate cut in a direction. The section through the indicatrix is an ellipse with axes  $n_x$  and  $n_y$ . The ray path both through the wave normal (WN) as shown (cf. Figure 7.4).

- Fig 7.4b와 동일하게 작도됨
- 가장 일반적인 형태의 빛 투과
- WN : 굴절 안됨
- $n_x < n_x' < n_y$
- $n_y < n_y' < n_z$
- 진동방향 // 타원의 축

### Crystallographic orientation of indicatrix Axes

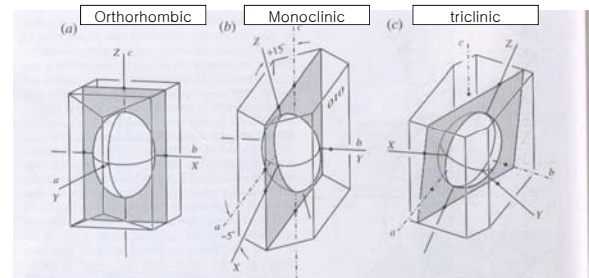


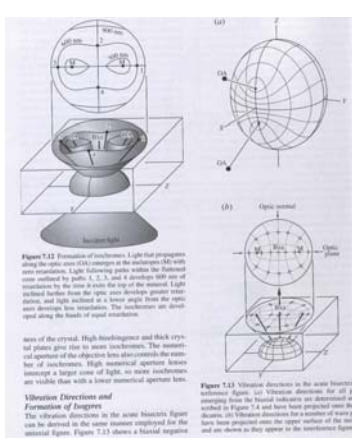
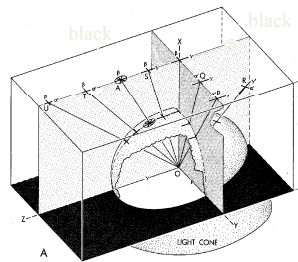
Figure 7.10 Relationship between crystal axes and indicatrix axes. The optic planes are shaded. (a) Orthorhombic. Crystal axes and indicatrix axes coincide. (b) Monoclinic. The  $b$  crystal axis coincides with one of the indicatrix axes. The other axes do not coincide except by chance. In this case  $b = Y$  so the optic plane is parallel to (010). If  $b = X$  or  $Z$ , then the optic plane is at right angles to (010). (c) Triclinic. None of the crystal axes coincide with indicatrix axes except by chance.

### Biaxial Interference Figures

$B_{xa}$  figure ( $B_{xa}$  is vertical on stage)

As in uniaxial, condensing lens causes rays to emanate out from O

- OX  $\rightarrow$  OS  $\rightarrow$  OA
- results in decreasing retardation (color) as  $\gamma \rightarrow \beta$
- OA  $\rightarrow$  OT  $\rightarrow$  OU
- Increase again, but now because  $\beta \rightarrow \alpha$
- OX  $\rightarrow$  OQ  $\rightarrow$  OP
- $\Rightarrow$  incr retardation (interference colors)
- OR is random with  $\alpha'$  and  $\gamma'$



### 간섭상

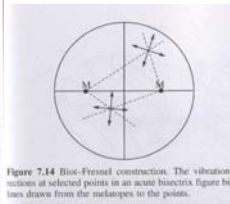
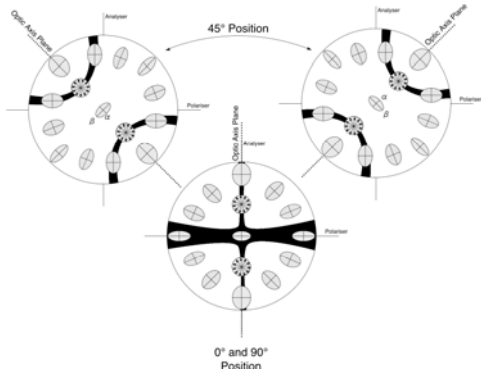
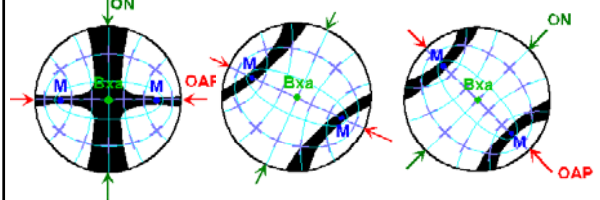


Figure 7.14 Biot-Fresnel construction. The vibration directions of selected points in an acute bisectrix figure being lines drawn from the melatopes to the points.

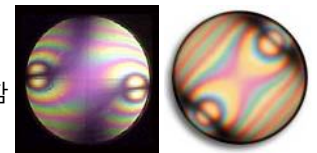
### Acute bisectrix figure

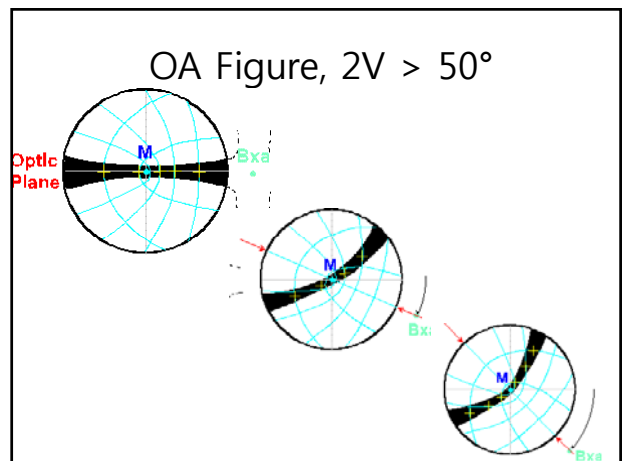
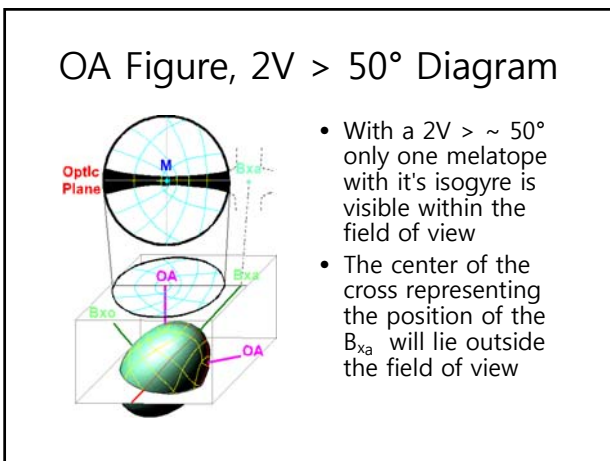
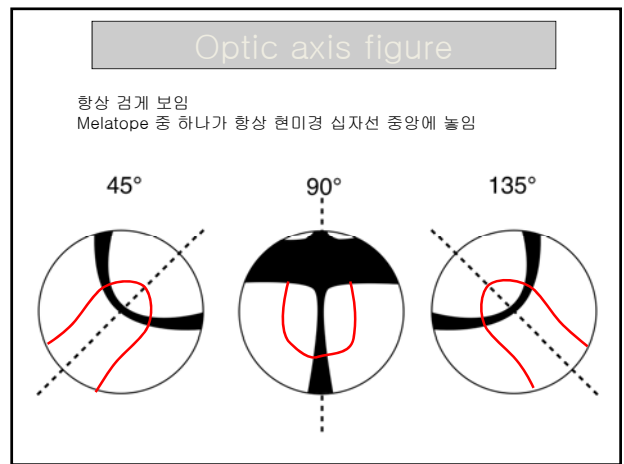
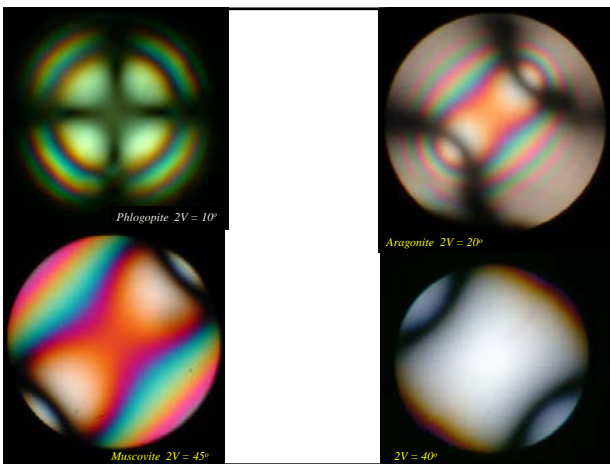
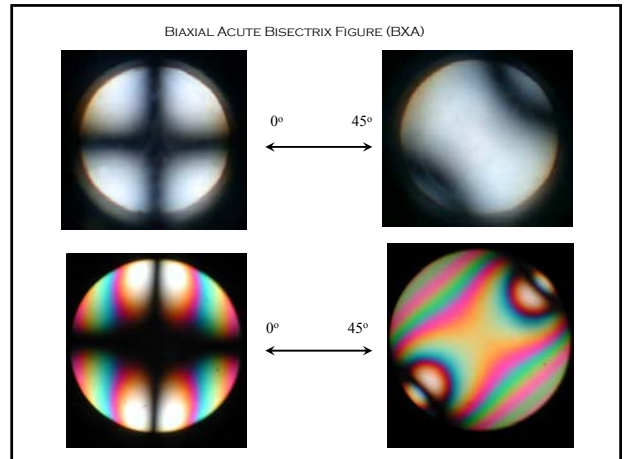
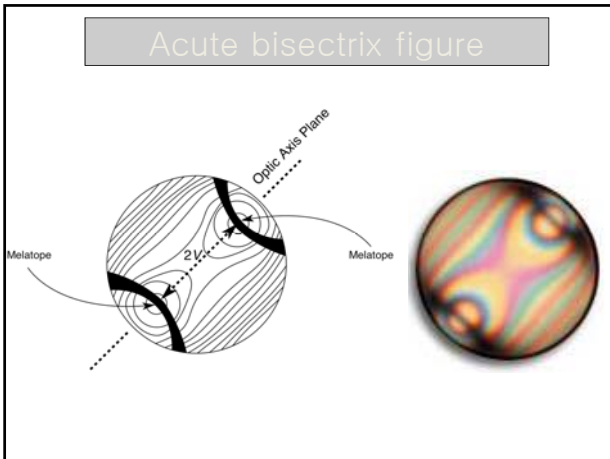


### $B_{xa}$ figure ( $2V < 40^\circ$ )



- M : melatope
- Isochrome : 8자 모양
- Isogyre : 회전시 변화함





### Obtuse Bisectrix Figure, $B_{X_0}$

- $B_{X_0}$  가 스테이지의 수직으로 놓인 경우
- M이 시야 밖에 존재
- 약간만 스테이지를 회전시켜도 Isogyre가 사라짐

### Obtuse Bisectrix Figure, $B_{X_0}$

### ON Figure

- The vibration directions for the two rays exiting in figure are similar to those for a uniaxial flash figure
- When the X & Z indicatrix axes parallel the polarization directions, the flash figure is a broad fuzzy cross with only the outer edges of each quadrant of the field of view allowing some light to pass

### ON Figure, Small Rotation

### Optic sign determination

**Positive**

**Negative**

BURP still applies!

### DETERMINATION OF OPTIC SIGN WITH A BXA INTERFERENCE FIGURE:

The optic sign of a biaxial mineral is commonly determined by using the accessory plate to distinguish the relative orientations of  $N_{big}$  or  $N_{small}$  in the region between the two parabolic isogyres of the BXA interference figure in the  $45^\circ$  position, as compared to the regions outside them. In the  $45^\circ$  position,  $\eta_b$  is oriented between the two isogyres, while either  $\eta_x$  (+) or  $\eta_y$  (-) is oriented along the optic plane joining the two optic axes and thus bisecting the two parabolic isogyres. The question then becomes; is  $\eta_b$  equal to  $N_{big}$  or  $N_{small}$  compared to the vibration direction along the optic plane.

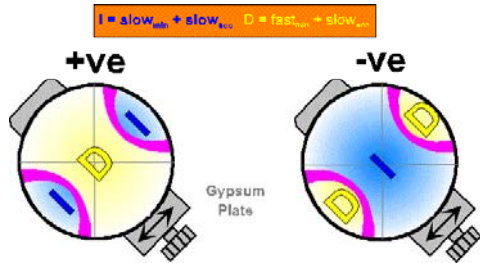
**Biaxial positive**

**Biaxial negative**

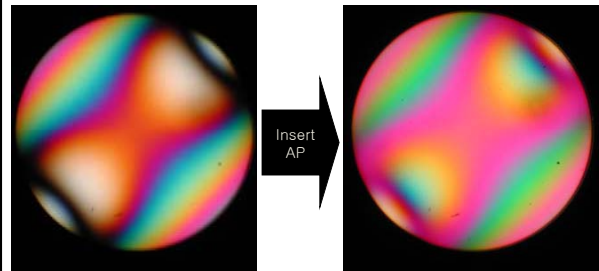
If  $\eta_b$  is  $N_{big}$ , then the other is  $\eta_x$ , and you are looking down  $\eta_y$  and thus the mineral is biaxial positive.  
 If  $\eta_b$  is  $N_{small}$ , then the other is  $\eta_y$ , and you are looking down  $\eta_x$  and thus the mineral is biaxial negative.



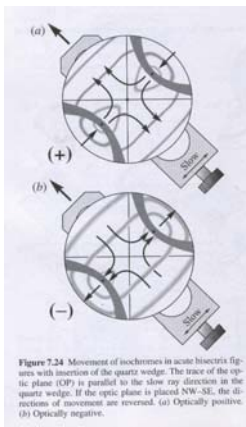
### Biaxial optic sign acute bisectrix figure



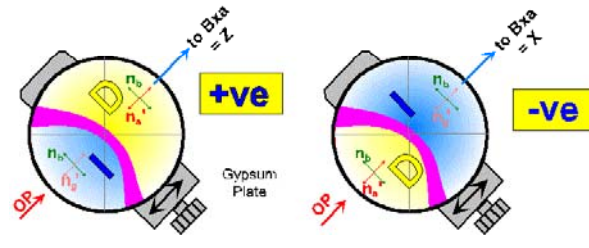
### Biaxial negative figure



### Qtz wedge



### Optic axis figure



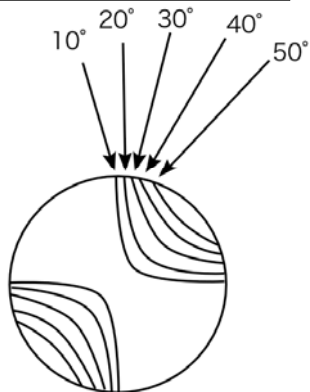
### 2V determination

Separation of melatopes is a measure of 2V

Angular width of field of view is around 55-60°.

**Remember:** if mineral is positive, you are measuring 2V<sub>γ</sub>.

If negative, you are measuring 2V<sub>α</sub>.



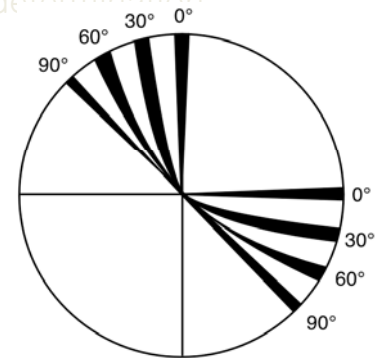
### Optic sign and 2V determination

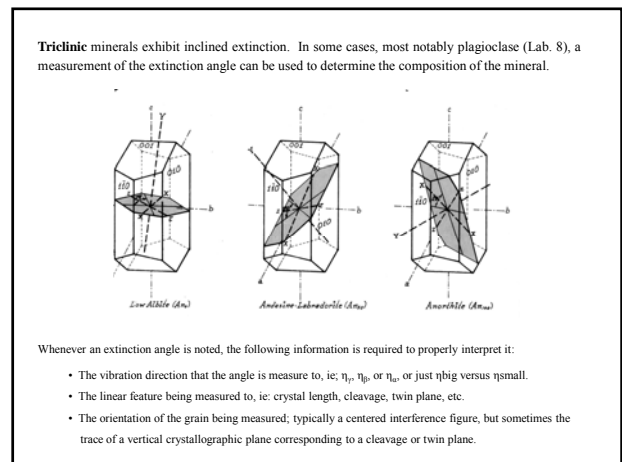
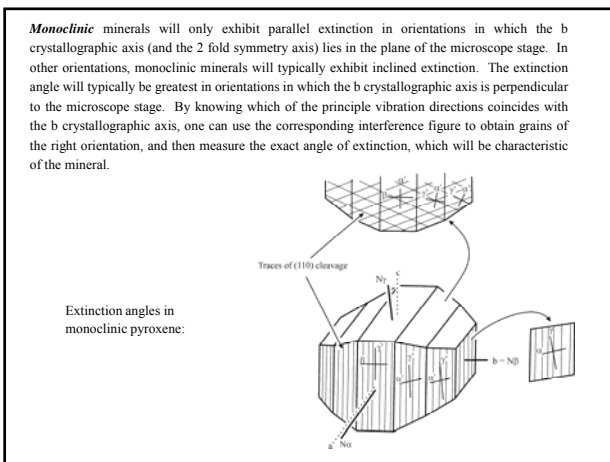
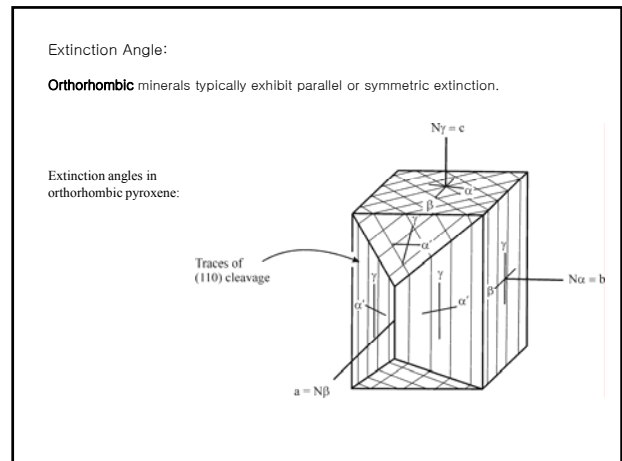
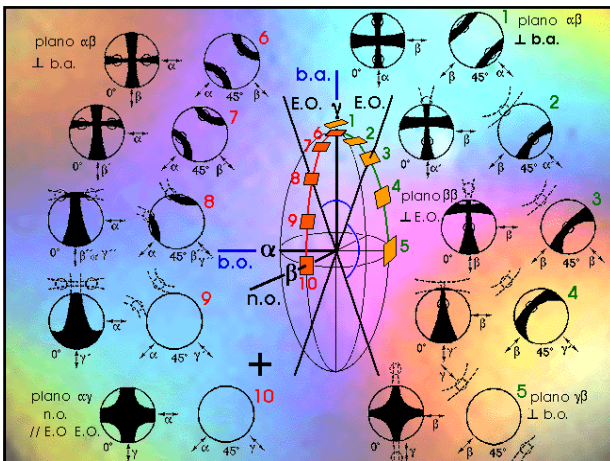
As long as the isogyre curves in the 45° position, the rest of the figure can be imagined and the BURP rule applied.

Curvature varies with 2V.

2V = 0 Isogyre curves through 90° (i.e. is a uniaxial figure).

2V = 90° Isogyre shows no curvature (sign cannot be determined, since it is neither +ve or -ve).





### Pleochroism in biaxial minerals

- Since 3 indices of refraction; 3 colors (1 per axis)
- Light parallel to X axis is least strongly absorbed. Z is most strongly absorbed
- Hornblende x = yellow y = pale green, z = dark green

### Pleochroism in biaxial minerals

- For Y, find grain nearly isotropic, uncross polars
- For X and Z, find grain with highest interference colors
- Rotate to extinction, then 45° clockwise, slide in accessory plate, determine if addition or subtraction
  - If color increases, addition, slow ray, Z ray
- Rotate another 45° clockwise, uncross polars and note color
- For other axis, rotate 90° from here